

## Recreating the state of the radiation belts for the last 30 years

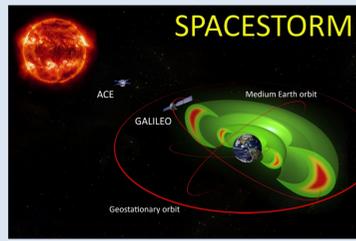
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### 1. Introduction

Medium Earth Orbit (MEO) is becoming increasingly important

- Galileo, GPS, O3B
- Electric orbit raising
- Limited data on high-energy electrons at MEO
- No data set covers a whole solar cycle



### 2. The BAS Radiation Belt Model (BAS-RBM)

Physics-based model, includes:

- Transport across the radiation belts
- Interactions with electromagnetic waves
  - lower band, upper band and low-frequency chorus
  - EMIC waves
  - plasmaspheric hiss and lightning-generated whistlers
- Collisions between the electrons and the atmosphere
- Losses to the magnetopause

$$\frac{\partial f}{\partial t} = \frac{1}{g(\alpha)} \frac{\partial}{\partial \alpha} \left[ g(\alpha) \left( D_{\text{diff}} \frac{\partial f}{\partial \alpha} + D_{\text{ad}} \frac{\partial f}{\partial E} \right) \right] + \frac{1}{A(E)} \frac{\partial}{\partial E} \left[ A(E) \left( D_{\text{diff}} \frac{\partial f}{\partial \alpha} + D_{\text{ad}} \frac{\partial f}{\partial E} \right) \right] + L^2 \frac{\partial}{\partial L} \left[ \left( \frac{1}{L^2} D_{LL} \frac{\partial f}{\partial L} \right) \right] - \frac{f}{\tau}$$

$$g(\alpha) = \sin 2\alpha (1.3802 - 0.3198(\sin \alpha + \sin \alpha^{1/2}))$$

$$A(E) = (E + E_0)(E + 2E_0)^{1/2}$$

### 3. Outer boundary condition

Need a data set that covers 30 years

- GOES > 2MeV electron flux

GOES provides:

- Integral flux
- At GEO - varying L\*
- Only one energy

Model requires:

- Differential flux
- At fixed L\*
- A range of energies

Need to

- Map to fixed L\* to remove diurnal variation
- Approximate differential energy spectrum from one integral flux measurement

### 3a. Map to fixed L\*

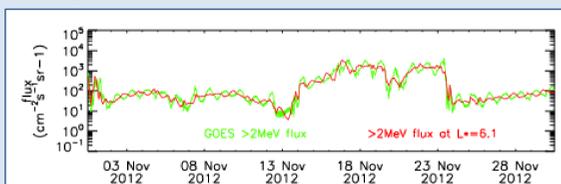
Statistical Asynchronous Regression [O'Brien et al., 2001]

- Determines the relationship between two time varying quantities, without the need for simultaneous measurements of both quantities
- Finds a function that maps the flux measurement at any MLT, to the flux that would be measured by the same instrument at a chosen local time.

Procedure

- Separate mappings for each GOES spacecraft
- Average GOES > 2 MeV flux into 2 hour MLT bins
- Calculate MLT & Kp dependent corrections
- Calculate mappings to both dawn and dusk
  - Map flux to dawn and dusk and then average

Example: November 2011 – GOES 15

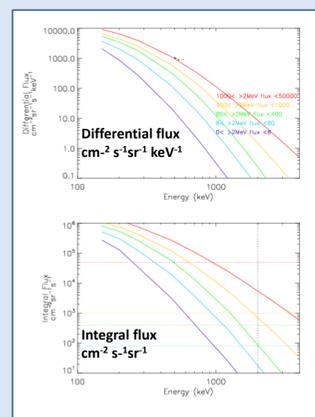


### 3b. Defining the spectrum

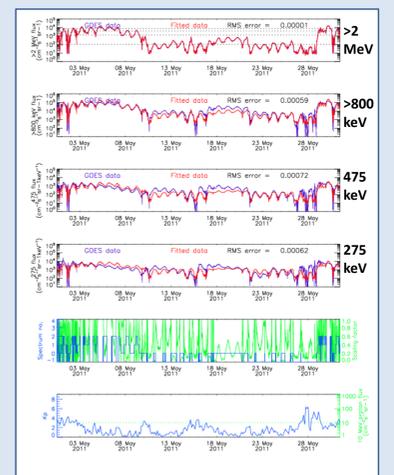
GOES provides one integral energy flux - model needs spectrum (~200 keV ≤ E ≤ ~30 MeV)

Use GOES 15 MAGED to define spectra for use with all GOES spacecraft

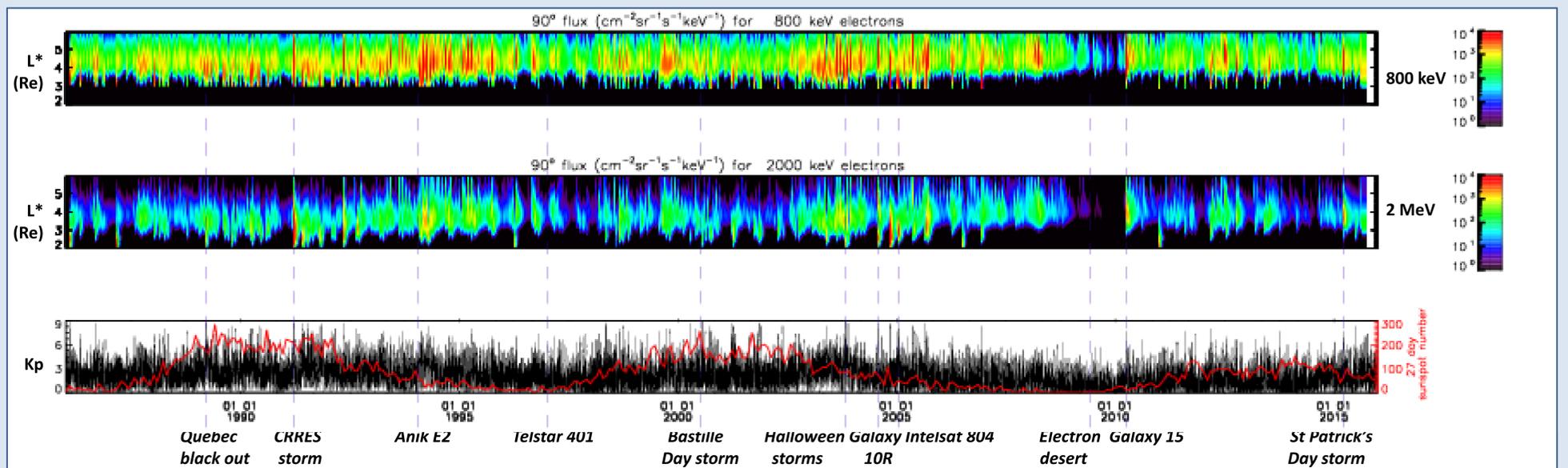
- Differential flux at 150, 275 and 475 keV from MAGED
- Estimate differential flux from >800keV and >2MeV flux:  $J(1265 \text{ keV}) = \frac{I(800) - I(2000)}{1200}$
- Bin flux by level of >2 MeV flux
  - Spectrum shape depends on activity
- Fit kappa distribution to phase-space density
- Get differential and integral flux spectra



Spectra used on outer boundary



Comparison of fitted spectra and data May 2011



### 4. Evaluation using GIOVE-B data

Galileo In-Orbit Validation Element-B (GIOVE-B)  
~4 years of data (May 2008 – July 2012)

Standard Radiation Environment Monitor (SREM), [Evans et al., 2008].

TC1 channel E > 2 MeV

TC3 channel E > 800 keV.

Use response functions to convert model output to SREM count rates

Giove-B response functions not available - use Rosetta response functions

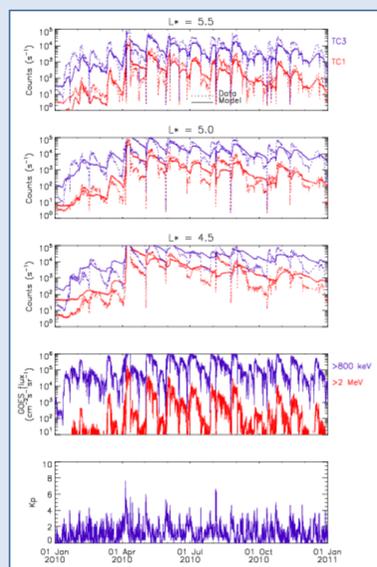
Evaluate simulation using skill scores

$$SS = 1 - \frac{\sum_i (X_i - Y_i)^2}{\sum_i (X_i - \bar{X})^2}$$

| Year | TC1 at L*=5 |
|------|-------------|
| 2008 | 0.72        |
| 2009 | 0.83        |
| 2010 | 0.74        |
| 2011 | 0.58        |
| 2012 | 0.71        |

| L*  | TC1 in 2010 |
|-----|-------------|
| 4.5 | 0.67        |
| 5   | 0.74        |
| 5.5 | 0.71        |

Skill scores



Comparison of model and GIOVE-B data

### 5. Conclusions

- Simulated the radiation belts between L\* = 2 - 6 for the last 30 years
  - New method of deriving boundary conditions from GOES data
  - First long term simulation of the radiation belts (we think!)
- Considerable long and short-term variation throughout the belts
  - Solar cycle variations are clearly visible
  - Fast solar wind streams in the declining phase produce more intense fluxes throughout the belts
  - Low fluxes at start of solar cycle
- Results compared with the count rates from SREM on the GIOVE-B
  - Annual skill score usually exceeds 0.5, often exceeds 0.7.
- Flux spectrum along a Galileo-type orbit for 30 years will be available on the SPACESTORM website by end March 2017
  - Resource for satellite designers, operators and insurers